Hudson Park High School



GRADE 11 MATHEMATICS JUNE EXAMINATION PAPER 2

Marks

100

Time

2 Hours

Date

3 June 2019

Exam

PHL

Moderator(s)

SLT, FRD.

INSTRUCTIONS

- 1. Illegible work, in the opinion of the marker, will earn zero marks.
- 2. Number your answers clearly and accurately, exactly as they appear on the question paper.
- 3. <u>NB</u> START <u>EACH QUESTION</u> AT THE <u>TOP OF A NEW PAGE</u>.
 - LEAVE <u>2 LINES OPEN BETWEEN</u> EACH OF YOUR <u>ANSWERS.</u>
- 4. NB Fill in the details requested on the front of the question paper and Answer Booklet.

Hand in your submission in the following manner:

- Question paper (on top)
- Answer pages in order (below).
- 5. Employ relevant formulae and show all working out. Answers alone may not be awarded full marks.
- 6. (Non-programmable and non-graphical) Calculators may be used, unless their usage is specifically prohibited.
- 7. Round off answers to 2 decimal places, where necessary, unless instructed otherwise.
- 8. If (Euclidean) Geometric statements are made, reasons must be stated appropriately.

QUESTION 1 [10 marks]

1. The following points have been scored by the Hudson Park High School rugby team in 12 matches.

11;15; 17; 18; 20; 23; 28; 29; 35; 35; 35, 40

1.1 Calculate

- 1.1.1 Mean (2)
- 1.1.2 Mode (1)
- 1.1.3 Median (1)
- 1.1.4 interquartile range (3)
- 1.2 Represent the match points by means of box-and-whisker diagram. (3)

QUESTION 2 [7]

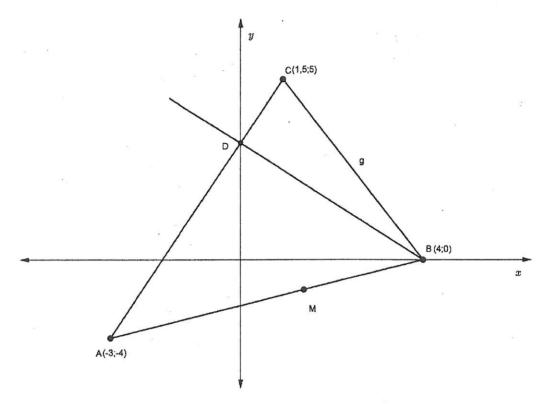
2. The following table represents the ages of tourists in a group.

Age	Frequency (f)
$20 \le x < 30$	5
$30 \le x < 40$	16
$40 \le x < 50$	12
$50 \le x < 60$	9
$60 \le x < 70$	8

- 2.1 How many tourists were there in a group? (1)
- 2.2 Calculate the average age of the tourist. (4)
- 2.3 Determine the interval in which the seventh decile lies. (2)

QUESTION 3 [12]

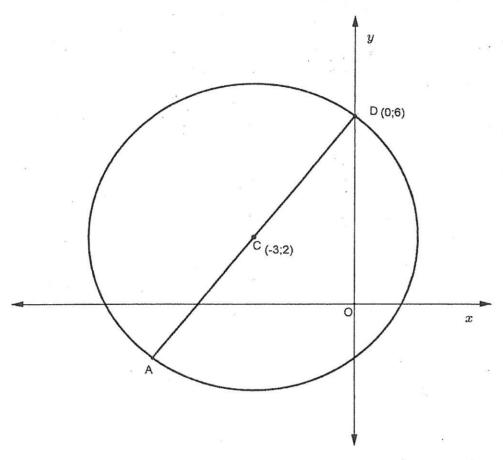
3. In the diagram below, ABC is a triangle with coordinates A(-3;-4), B(4;0) and C($1\frac{1}{2}$; 5), M is the midpoint of AB and D is a point of intersection of AC and the y – axis.



- 3.1 Determine the following
- 3.1.1 the gradient of line AC. (2)
- 3.1.2 length of BC to 2 d. p. (2)
- 3.1.3 the coordinates of M the midpoint of line AB. (2)
- 3.1.4 the coordinates of D. (3)
- 3.2 Show that BD \perp AC. (3)

QUESTION 4 [9]

In the diagram below C(-3;2) is the centre of a circle and D(0; 6) is given.



- 4.1 Give a reason why CD = CA. (1)
- 4.2 Calculate the coordinates of A. (2)
- 4.3 Determine the gradient of CD. (2)
- 4.4 Determine the equation of the line (not shown) parallel to CD and passing throwugh the point (-6;5). (3)
- 4.5 Now, write your answer to 4.4 in the form ax + by + c = 0.

 where a, b, c are integers. (1)

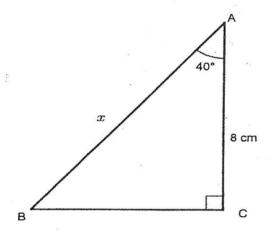
QUESTION 5 [11]

5.1 Solve for θ where $\theta \in (0^{\circ}, 90^{\circ})$

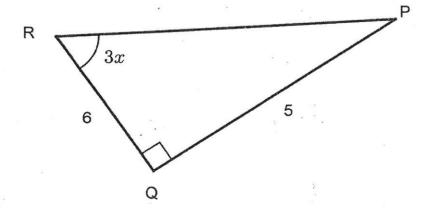
$$5.1.1 \quad \frac{\sin\theta}{2} = \frac{\sin 50^{\circ}}{6} \tag{2}$$

5.1.2
$$8^2 = 10^2 + 9^2 - 2 \times 10 \times 9 \times \cos\theta$$
. (2)

5.2 Calculate the value of x



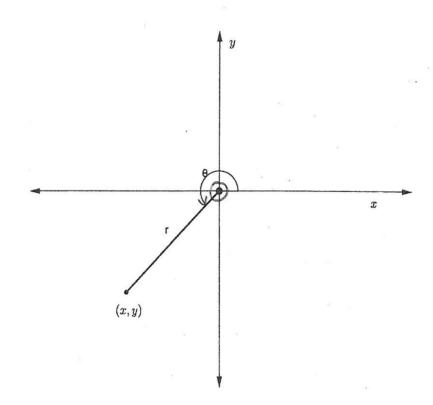
5.2.2



5.3 Evaluate, if
$$\theta = 15^{\circ}$$
, $\frac{3\tan^2 \theta}{\cos 2\theta - 1}$ (2)

QUESTION 6 [12]

- 6. CALCULATORS MAY NOT BE USED IN THIS QUESTION.
- 6.1 Evaluate the following
- 6.1.1 $\tan 30^{\circ}$ (2)
- $6.1.2 \sin 45^{\circ}$ (2)
- 6.2 Given
 - $\bullet \sin\theta = \frac{-5}{13}$
 - $tan\theta > 0$
- 6.2.1 Explain why θ must be an angle in Quadrant 3. (2)
- 6.2.2 Use the initial given information to calculate x, y and r in the associated diagram below. (3)



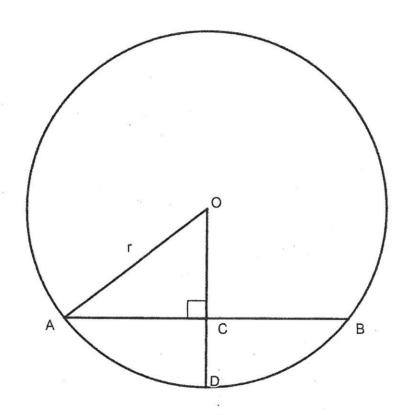
6.2.3 Hence, determine
$$\sin^2 \theta + \cos^2 \theta$$
. (3)

QUESTION 7 [7]

- 7 Complete the following theorem.
- 7.2 In the diagram, O is the centre of the circle. Chord AB = 24cm.

 OC \perp AB. If CD = 8cm, calculate the length of the

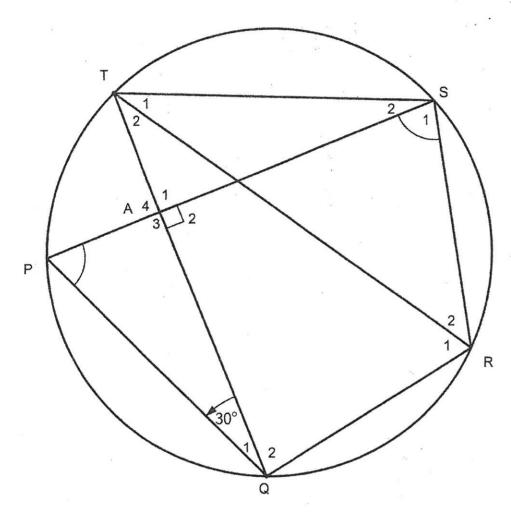
radius of the circle. Let OA = r. (5)



QUESTION 8 [10]

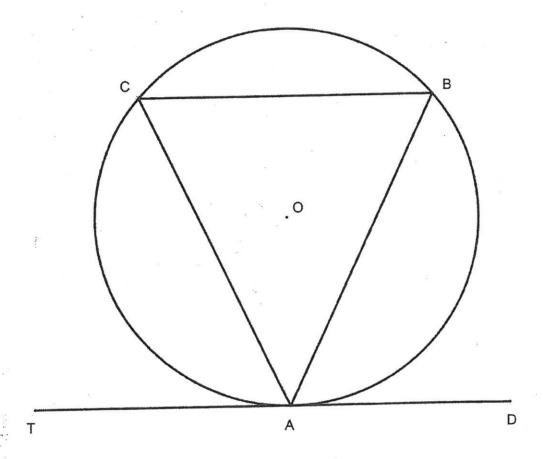
8. In the diagram below, TR is a chord of the circle PQRST.

QAT
$$\perp$$
 PAS, $\widehat{Q}_1 = 30^{\circ}$, $\widehat{P} = \widehat{S}_1$

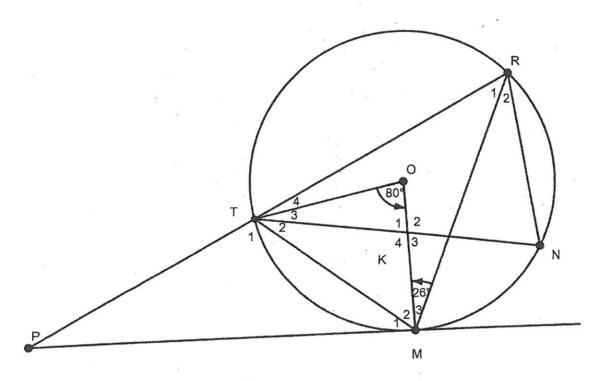


- 8.1 Name stating reasons, three angles equal to 60°. (4)
- 8.2 Calculate the size of angle $Q\widehat{R}S$. (2)
- 8.3 Prove that PS \parallel QR. (2)
- 8.4 Prove that TR is a diameter of the circle. (2)

9.1 TAD is a tangent to the circle centre O. Prove the theorem which states that $B\widehat{A}D = A\widehat{C}B$. (7)



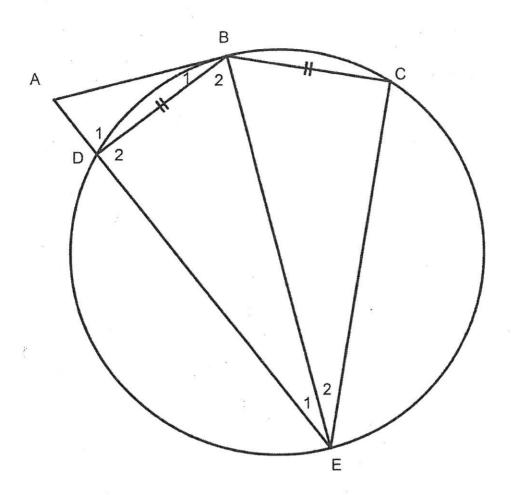
In the diagram below, O is the centre of the circle TRNM. RT produced meets tangent MP at P. OM intersects TN at K. K is the midpoint of TN $\widehat{MOT} = 80^{\circ}$, $\widehat{M}_3 = 26^{\circ}$.



Calculate with reasons

9.2.1
$$\widehat{M}_1$$
 (4)
9.2.2 \widehat{N} (4)
9.2.2 \widehat{T}_3 (3)

10. AB is a tangent to the circle. DB = BC.



10.1 Prove that
$$\widehat{B}_1 = \widehat{E}_2$$
. (2)

10.2 Complete
$$\widehat{D}_1 = \dots$$
 (2)

[TOTAL 100 MARKS]